Peano continua with self regenerating fractals

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We deal with the question posed by M. Hata: is every Peano continuum a topological fractal? A compact space X is a topological fractal if there exists F, a finite family of selmaps on X that makes X an invariant set for the family F and satisfies the condition that for every open cover U of X there is a natural number n such that for any maps $f_1, ..., f_n$ the image $f1 \circ \cdots \circ f_n(X)$ is contained in some set from U. We show that a Peano continuum is a topologica l fractal if it contains so-called self regenerating fractal with nonempty interior. A Hausdorff topological space A is a self regenerating fractal if for every non-empty open subset U, A is a topological fractal for some family of maps that are constant outside of U.