Strengthening of de Groot's and Spadaro's inequalities for Urysohn spaces

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In 1965, de Groot proved that if X is a Hausdorff space, then $|X| \leq 2^{hL(X)}$, where $hL(X)$ is the hereditary Lindelöf degree. In 2011, Spadaro improved de Groot's inequality by showing that for every Hausdorff space X we have $|X| \leq 2^{L(X)F(X)\psi(X)}$, where $L(X)$ is the Lindelöf degree of X, $F(X)$ is the supremum of the cardinalities of the free sequences in X, and $\psi(X)$ is the pseudocharacter of X.

Recently Angelo Bella improved de Groot's and Spadaro's inequalities for the class of regular T_1-spaces by showing that for such spaces X we have $|X| \leq hL(X)^{F(X)\psi(X)}$ and he asked if the same inequality is true for every Hausdorff space X.

In this talk we will mention several results strengthening de Groot's, Spadaro's, or Bella's inequalities, most of which for the class of Urysohn spaces.